

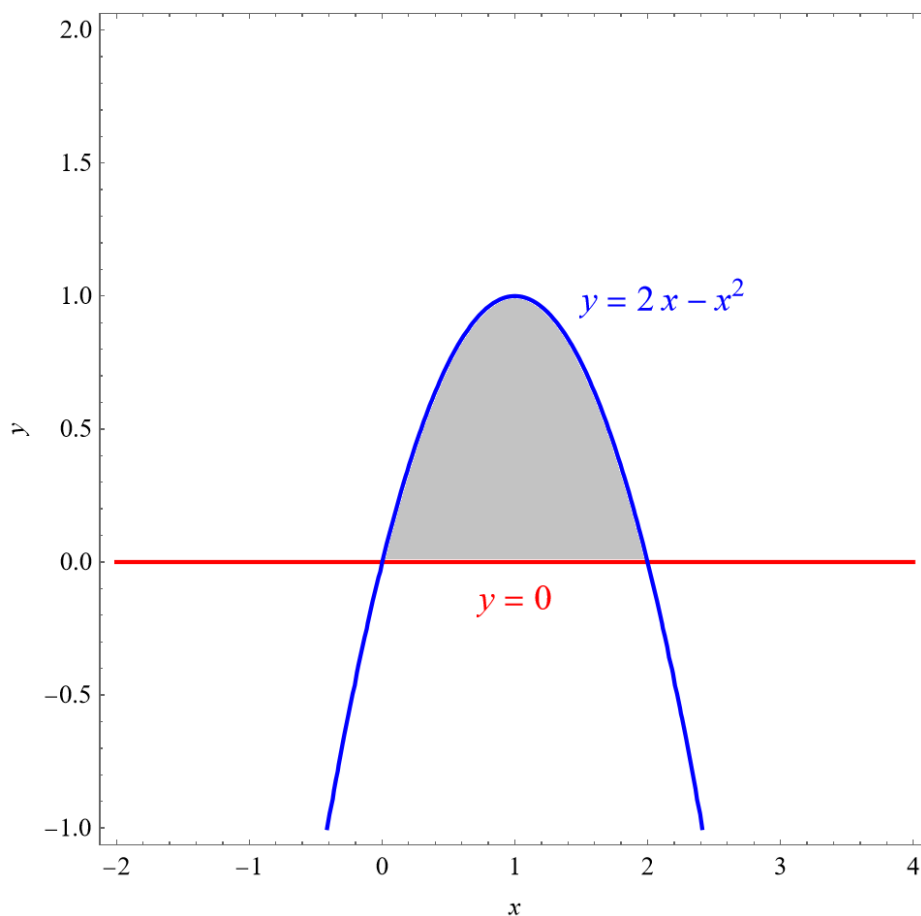
Exercise 48

Sketch the region enclosed by the given curves and calculate its area.

$$y = 2x - x^2, \quad y = 0$$

Solution

Start by drawing the given curves in the xy -plane and shading the area they enclose.



The shaded area is calculated by integrating the height ($2x - x^2 - 0$) from the lowest value of x to the highest value of x that it occupies.

$$\begin{aligned} \text{Area} &= \int_{x_{\min}}^{x_{\max}} \text{Height } dx = \int_0^2 (2x - x^2) dx \\ &= \left(x^2 - \frac{x^3}{3} \right) \Big|_0^2 \\ &= \left[(2)^2 - \frac{(2)^3}{3} \right] - \left[(0)^2 - \frac{(0)^3}{3} \right] = \frac{4}{3} \end{aligned}$$